



WORKING PAPER SERIES

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Working paper 7

October 2007

www.recent.unimore.it

Dynamic Factor analysis of industry sector default rates and implication for Portfolio Credit Risk Modelling

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October 2007

Abstract

In this paper we use a reduced form model for the analysis of Portfolio Credit Risk. For this purpose, we fit a Dynamic Factor model, DF, to a large dataset of default rates proxies and macro-variables for Italy. Multi step ahead density and probability forecasts are obtained by employing both the direct and indirect method of prediction together with stochastic simulation of the DF model. We, first, find that the direct method is the best performer regarding the out of sample projection of financial distressful events. In a second stage of the analysis, we find that reduced form Portfolio Credit Risk measures obtained through DF are lower than the one corresponding to the Internal Ratings Based analytic formula suggested by Basel 2. Moreover, the direct method of forecasting gives the smallest Portfolio Credit Risk measures. Finally, when using the indirect method of forecasting, the simulation results suggest that an increase in the number of dynamic factors (for a given number of principal components) increases Portfolio Credit Risk.

Keywords: Dynamic Factor Model, Forecasting, Stochastic Simulation, Risk Management, Banking
JEL codes: C32, C53, E17, G21, G33

Acknowledgements: The authors wish to thank, for their comments, seminar participants at the Department of Economics, University of Birmingham; participants of the XV International Conference on Banking and Finance, (Tor Vergata University), of the EC² symposium in Rotterdam (Erasmus University, December 2006), of the 10th Conference of the Swiss Society for Financial Market Research, SGF, in Zurich, of the workshop on Computational Finance and Econometrics, CFE, (Geneva, April 2007), of the European Econometric Society meeting (Budapest, August 2007), of the workshop on Default Risk and Financial Distress in Rennes (September 2007) and of the Dynamic Factor workshop in Queen Mary, London (October 2007). In particular, the authors wish to thank Claudia Girardone, Lucia Alessi, Matteo Barigozzi and Marco Capasso, Stephan Kessler, Ana Maria Fuertes, Olivier Renault, Franck Moraux, H. Pesaran and J. Bai for helpful comments. All the computations have been carried using Gauss, with the exception of the pooled unit root test on the idiosyncratic component of the factor model for which we used the MATLAB routine developed by Serena Ng. The views in this paper are those of the authors. The usual disclaimer applies: all remaining errors are the sole responsibility of the authors.

1. Introduction

In this paper we empirically investigate industry sector specific default rates proxies in Italy, taking into account their interaction with business cycle credit drivers. Recent studies (reviewed below) show that defaults (and credit spreads) tend to co-move with macro-economic variables, and this has important consequences for credit risk management as well as for regulation and systemic risk management. The interaction between financial fragility of the financial/non financial corporate sector and the business cycle is explored in Koopman and Lucas (2005) and in Hoggarth et al. (2005). In particular, Koopman and Lucas (op. cit.) use a multivariate unobserved components model to disentangle credit and business cycles in the U.S., using real GDP, an aggregate credit spread, and an aggregate business failure rate for non financial corporates. Hoggarth et al. (2005) focus on the interaction between an indicator of banks' fragility, the write-off to loan ratio and key macroeconomic variables.

Other studies prefer to focus on the impact of key macro-variables on the fragility of financial and non financial corporates (without allowing for feedback effects from financial fragility to the macroeconomy). A cointegrating VAR model by Alves (2004) to examine the effects of macro-variables on industry sector Expected Default Frequency, EDF (measured through a structural form credit risk model) and the focus is on EU non financial corporates fragility. The impact effect of key macro-variables on an indicator of bank fragility (e.g. loan-loss provisions) is analysed by Pain (2004), using panel regression analysis, and focussing on a number of UK banks. The focus of Elsinger, et al. (2002) is the fragility of the Austrian banking sector and, for this purpose, they analyse the effect of macroeconomic shocks (such as interest rate shocks, exchange rate and stock market movements, as well as shocks related to the business cycle) on a matrix of Austrian interbank positions. Specifically, the authors (op. cit.) are able to assess the probability of individual bank failures in response to a series of macroeconomic factors while at the same time taking into account the effect that these failures have on the rest of the banking system. This model thus decomposes bank defaults into those that arise directly and those that are a consequence of contagion. Carling et al. (2006) estimate a duration model to explain the survival time to default for borrowers in the business loan portfolio of a major Swedish bank over the period 1994-2000. The model takes into account both firm-specific characteristics, such as accounting ratios, and the prevailing macroeconomic conditions.

If the focus is on the composition of a bank loan portfolio, then measures of risk for a bank loan portfolio can be considered to measure bank fragility. Pesaran et al. (2006), using stock returns as proxies of firm asset values, simulate a global VAR model to generate macro scenarios

and evaluate the impact on the portfolio loss. While the Pesaran et al. (op. cit.) method has the flavour of a structural form Portfolio Credit Risk model, the studies of Hamerle et al (2004) and Virolainen (2004) are reduced form models in which the simulation the bank loan Portfolio Loss density is obtained after estimating the impact of key macro variables on industry sector default rates. Given that we observe historical industry sector default rates, in our study we concentrate on a reduced form modelling for the purpose of Portfolio Credit Risk analysis similar to the studies of Credit Portfolio View (see Wilson, 1997), of Virolainen (2004) and of Hamerle et al. (2004). In particular, our focus is on the study of the capital requirement (through the cycle) using multiple factors to model the Unconditional Portfolio Loss density. More specifically, we fit a Dynamic Factor model (see Stock and Watson, 2002), DF, to a large dataset which includes proxies of an aggregate default rate, and of 23 sector specific default rates and a large number of macro-variables for the Italian economy (for a total of 103 constituents). We produce multiple step ahead density forecasts through either the direct method or the indirect method of prediction (see Marcellino et al, 2005). While the former method relies on simulation of principal components (e.g. the proxies of static factors), the latter method relies on simulation of dynamic factors. The extraction of common factors underlying the dynamics of the observables entering in the large dataset we consider allows to take into account the joint interaction of default rates with proxies of macroeconomic activity. The mutual interaction between default and the state of macro-economy has been studied through state space modelling of an unobserved component model, by Koopman and Lucas (2005) and by Koopman et al. (2005), using aggregate data for the level of default rates and of the real economic activity in the US. Given the short time series available for default rates (starting from 1990, on quarterly basis) and the large number of cross sections, the DF model employed in our study allows a feasible modelling of default correlation and of the Portfolio Loss density. Specifically, in this paper, we investigate the sensitivity of Portfolio Credit Risk measures to DF model specifications and to different method of forecasting. In particular, using a direct method of forecasting, we simulate the density prediction of default rates and of the Portfolio Loss using Gaussian shocks to static factors (e.g. the principal components); whereas, when using the indirect method of forecasting, we simulate the density prediction of default rates and of the Portfolio Loss using Gaussian shocks to dynamic factors. Also, while most of the aforementioned studies provide in sample forecasting analysis of financial fragility indicators for sector specific firms, in this paper we carry out of sample forecasting analysis. Specifically, we compare the forecasting performance of the Dynamic Factor model regarding distressful events affecting sector specific default rates with the one associated with a naïve predictor and to a reduced form modelling approach along the lines of Credit Portfolio View (see Wilson, 1997). The empirical findings show that the best performer in

terms of forecasting financially distressful periods is the direct method of prediction through shocks to the principal components. The simulation of the portfolio loss density through Dynamic Factor modelling, suggests a value of the minimum capital requirements lower than the one obtained by the analytic formula recommended by Basel 2. Finally, when using the indirect method of forecasting, the simulation results suggest that an increase in the number of dynamic factors (for a given number of principal components) increases Portfolio Credit Risk.

The outline of the paper is as follows. Section 2 describes the default correlation issue; Section 3 describes the Dynamic Factor model. Sections 4 and 5 describe the stochastic simulation exercise and the probability forecasts, respectively. Section 6 describes the data and discusses the empirical results. Section 7 concludes.

2. Default rates correlation and Portfolio Loss density

In light of the Basel 2 accord which provides for greater sensitivity of capital requirements to the credit risk inherent in bank loan portfolios, there has been an extensive research on Portfolio Credit Risk. A crucial input of a portfolio credit risk model, PCR, is the appropriate characterisation of default correlations to obtain the portfolio loss density forecast with the relevant percentile (e.g. the minimum capital requirement). The structural form approach to model a large bank loan portfolio loss density (see the Creditmetrics approach developed by Gupton et al., 1997, and, more recently, see Pesaran et. al, 2006, among the others) relies upon the simulation of extreme co-movements in stock returns (used as proxies of firm asset value) through the generation of scenarios described by shocks to common observable factors related to market variables and/or to macro credit drivers. If historical default rates are available, then it is possible to follow a reduced form modelling approach to Portfolio Credit Risk. In particular, few studies generate default rates density forecasts (and, consequently, the Portfolio Loss density forecast) calibrating upon the estimated parameters of a regression model fitted to historical default rates. For instance, the study of Hamerle et al. (2004) use a logit regression to predict default rates (for few macro-sectors of the German economy) through the past values of observable macro-credit drivers and the authors (op. cit.) model the random effects through an unobservable common shock. White noise Gaussian random draws are the realisations of the unobservable common shock and they allow to build the density forecast of default rates. The study of the Portfolio Loss density forecast in Virolainen (2004) is based upon the SUR estimation of a system of equations explaining logit transformed industry sector default rates for the Finnish economy through common observable factors. These are macro time series and they are modelled through an AR(2) process. While in Hamerle et al. (op. cit) and in Virolainen (2004), the focus is on the causality direction going from the macro-credit drivers to default rates, the

mutual interaction between defaults and state of macro-economy has been analysed by Koopman and Lucas (2005), and by Koopman et al. (2005), who focus on probit transformed default rates. Furthermore, in the studies of Virolainen (2004), Koopman and Lucas (2005), and of Koopman et al. (2005), the systemic shocks affecting default rates exhibit some degree of persistence in the propagation mechanism implying default correlation and Portfolio Loss density which vary according to the forecast horizon chosen. Contrary to the aforementioned studies we are interested in modelling the joint interaction among (proxies of) default rates for 23 different sectors of the Italian economy (in addition to the aggregate default rate), and between these default rates and a large number of macro-credit drivers. Given that the time series for default rates includes only 65 quarterly observations since 1990, and we consider a large number of cross sections, we simulate a Dynamic Factor model (see Stock and Watson, 2002) to obtain the density forecast of the different industry sector default rates. Finally, in line with Koopman and Lucas (2005), in order to obtain predictions of default rates bounded between zero and one, we consider a probit transform, which is related to the (average) distance to default for a specific industry sector. In particular, define def_t^i as the default rate for sector i , observed at time t . Following Finger (1999), and Lucas, Klaassen, Spreij and Straetmans (2001), for a large N , which is number of firms underlying the aggregate default rates per sector, the default rate per sector can be modelled as:

$$def_t^i = \frac{1}{N} \lim_{N \rightarrow \infty} \sum_{j=1}^N \mathbf{1}(A_{jt}^i < c^i)$$

where $\mathbf{1}(\cdot)$ is an indicator function, taking value 1 when A_{jt}^i , the asset value of firm j in sector i , at time t , falls below a threshold c^i (see Merton, 1974). Define $P[A_{jt}^i < c^i | z]$ as the probability of the firm asset value falling below threshold c^i conditional upon a realisation of z , e.g. the common systemic shock driving the firm asset value, then, for a large N , we can then write:

$$\begin{aligned} def_t^i &= \frac{1}{N} \lim_{N \rightarrow \infty} \sum_{j=1}^N P[A_{jt}^i < c^i | z] \\ &= \frac{1}{N} \lim_{N \rightarrow \infty} \sum_{j=1}^N \Phi \left(\frac{c^i - \beta^i z}{\sqrt{1 - \beta^{i2}}} \right) \\ &= \Phi \left(\frac{c^i - \beta^i z}{\sqrt{1 - \beta^{i2}}} \right) \end{aligned} \tag{1}$$

where β^i is the impact of the common systemic shock on the obligor firm asset value that belong to sector i ; Φ is the standard cumulative normal distribution, and its argument can be interpreted as the (average) distance to default in sector i . Therefore, the probit transform $y_t^i = \Phi^{-1}(def_t^i)$ can be related to the distance default for a specific industry sector.

3. Dynamic Factor model

Consider x_{nt} , which is the n cross-section dimensional dataset (observed at time t , for a total of T time series observations) including macro-economic credit drivers and the probit transform of sector specific default rates. The system (see Stock and Watson, 2002; Forni et al, 2005) is given by:

$$x_{nt} = CF_t + \xi_t \quad (2)$$

where F_t is the r dimensional vector of (static) factors; C is the $n \times r$ coefficient matrix of factor loadings, and by:

$$(I - \Gamma L)F_t = Ru_t \quad (3)$$

where $(I - \Gamma L)$ is a matrix lag polynomial and R measures the impact multiplier effect of the q dimensional vector of dynamic factors (common systemic shocks) u_t on F_t . As shown by Forni et al. (2005), the higher is the number of static factors (measured, in this study, by principal components) relative to the number of dynamic factors u , the higher is the degree of dynamic heterogeneity. In particular, as pointed out by Stock and Watson (2002), the number of static factors includes both current and past values of the dynamic factors, since $r \leq q(s+1)$, with s being the number of lagged dynamic factors. Combining (2) and (3) we obtain the (structural form) impulse response profile for each component in the panel x_{nt} :

$$C(I - \Gamma L)^{-1} R \quad (4)$$

In order to retrieve estimates of the coefficient matrices entering in the impulse response profile given by (4), we can proceed as follows. First, a consistent estimator of the static factor space is given by the first r principal components of x_{nt} , which is the panel of standardised observables (e.g. with mean zero and standard deviation equal to unity). Therefore, after demeaning the panel of raw data (subject to a transformation in order to get stationary series, see the footnote in data appendix)

and by dividing each component by the sample standard deviation, the principal components are given by:

$$F_t = \sqrt{T}W \quad (5)$$

where W is the $T \times r$ matrix having on the columns the eigenvectors corresponding to the first r largest eigenvalues of the XX' , with X being a $T \times n$ matrix of observables. The estimator of the matrix of factor loadings C is obtained by OLS regression of each of the observables in x_{nt} on the principal components F_t . The estimator of the coefficient matrix Γ is obtained by applying an OLS regression to each equation defining a VAR(1) on the principal components:

$$F_t = \Gamma F_{t-1} + \varepsilon_t \quad (6)$$

Finally, once we estimate Σ_ε , the sample covariance matrix of the reduced form innovation ε in (6), the structural form impact multiplier matrix R is given by KM , where:

- 1) M is the diagonal matrix having, on the diagonal, the square root of the q largest eigenvalues of Σ_ε , which is the covariance matrix of the residuals in (6).
- 2) K is the $r \times q$ matrix with columns given by the eigenvectors corresponding to the q largest eigenvalues of covariance matrix Σ_ε .

4. Simulation study of the unconditional portfolio loss density

In this section we describe how to obtain the density prediction of default rates through principal components using either the method of indirect or the method of direct forecasting (see Marcellino et al, 2005, although the focus of the authors is on point predictions). Given a one year forecast horizon for a bank and given data observed at quarterly frequency, we need to produce multi step ahead projections.

If we focus on the probit transform of default rates variables in the panel x_{nt} , then the impulse response profile in (4) can be used to retrieve the density prediction, through the indirect method of forecasting, for the default series proxies corresponding to sector i . Specifically, by rolling forward three times the one step ahead prediction, the conditional forecast of the probit transform of default rates is given by:

$$y_{t+4/t;U}^i = C^i \left[\Gamma^4 f_t + \Gamma^3 Ru_{t+1}^m + \Gamma^2 Ru_{t+2}^m + \Gamma Ru_{t+3}^m + Ru_{t+4}^m \right] \sigma^i + \mu^i \quad (7)$$

The entries in the coefficient matrix C_i are the standardised factor loadings of the principal components on the (standardised) default rates. The sample mean μ_i and sample standard deviation, σ_i , of the raw data for the probit transform of the default series are added back in order to obtain the prediction for the un-standardised level of (the probit transform of) default rates. The forecast in (7) is conditional on the information set available at time t (which, in this paper, is the sample of observations ending in first quarter of 2006) and on the scenario U given by the joint realisations of the common shocks from period $t+1$ till $t+4$. The latter are defined in (7) by $u_{t+1}^m, \dots, u_{t+4}^m$, (with the dimension of u being either one or two, according to the number of dynamic factors used) and they correspond to m^{th} draw from a standardised Gaussian distribution. Therefore, in line with common factors models of Portfolio Credit Risk, we model the systemic shocks as white noise. However, contrary to the study of Vasicek (2000), Schonbucker (2000), and in line with the study of Virolainen (2004) and of Pesaran (2006), the use of the indirect method of forecasting, allows some degree of persistence in the propagation mechanism (captured by the dynamic multipliers in equation 7) of the common shocks.

If we use the direct method of forecasting (which is more in line with the approach of Hamerle et al., 2003; 2004), then the conditional prediction for the probit transform of default rates is given by:

$$y_{t+4/t;U}^i = A^i \left[F_t + v_{t+4}^m \right] \sigma^i + \mu^i \quad (8)$$

where the loadings A^i have been obtained by regressing the probit transform of default rates on the principal components lagged four times, and F_t is the last observation for the estimated principal components. The dimension of the vector of Gaussian white noise disturbances v is equal to r , e.g. to the number of principal components.

Finally, the conditional prediction for the sector i level of default rates (bounded between 0 and 1) is given by:

$$def_{t+4/t;U}^i = \Phi(y_{t+4/t;U}^i) \quad (9)$$

where Φ is the cumulative Gaussian distribution function and its argument has been obtained either through equation (7) or (8).

If we want to calibrate the default rate density forecast of each obligor upon PD^{ij} , which is a given set of unconditional probability of defaults (which are the only determinants of the expected portfolio loss density), then we need to consider the following conditional projection:

$$def_{t+4/t;U}^{ij} = def_{t+4/t;U}^i - mean(def_{t+4/t;U}^i) + PD^{ij} \quad (10)$$

with $def_{t+4/t;U}^i$ given by (8). In this study we have chosen PD^{ij} to be the last observation in the sample for sector i default rate (hence it is the same across all the firms that belong to the sector i). Finally, the projection (four quarters ahead) of the portfolio loss density conditional upon the information set at time t and upon scenario U , is given by:

$$Loss_{t+4/t;U} = EAD^{ij} (1 - 0.55) * def_{t+4/t;U}^{ij} \quad (11)$$

where EAD^{ij} are the exposures of an Italian bank towards the different obligors. The value of 55% is the constant recovery rate chosen in the Basel 2 one factor model analytic formula for the computation of capital requirements.

The stochastic simulation involves 100000 joint random draws from $N(0,1)$ distribution which, in case of the indirect forecasting method, describe the realisations for the vector of common systemic shocks, u (which is either one dimensional or bi-dimensional), at the four different forecast horizons. The random draws from $N(0,1)$ distribution are in number of r (e.g. the number of principal components) when we consider the direct method of forecasting. Sorting, in ascending order, the values of the simulated density (and, assuming a constant recovery rate equal to 0.55 in line with the asymptotic one factor model of Basel 2), we obtain the unconditional portfolio loss density.

For the purpose of comparison, we consider the analytic, closed form formula for the unconditional Portfolio Loss density (and, in particular, the equation giving the Value at Risk quantiles) based upon the assumption of a single common factor underlying a structural form model of Portfolio Credit Risk. These analytic formulas are those provided by Schonbucher (2000) and Vasicek (2002) using the assumption of an infinitely granular homogeneous portfolio. The analytic formula implemented by Basel 2 is due to Gordy (2003) and it allows for heterogeneity in both the factor

loadings and in the unconditional probability of default. In particular, the computation of the economic capital charge for obligor j , ignoring a maturity adjustment, is given by:

$$UL_j = EAD_j \left\{ LGD * \Phi \left[\frac{(\Phi^{-1}(PD_j) + \sqrt{\rho_j} * \Phi^{-1}(0.999))}{\sqrt{1 - \rho_j}} \right] - PD_j \right\}$$

where EAD_j is the exposure at default of obligor j (expressed as a percentage of the total exposure); LGD is equal to one minus the constant recovery rate (set by the Basel 2 accord to 0.55); Φ is the standard cumulative Normal distribution; $\Phi^{-1}(\cdot)$ is the inverse of the cumulative Normal distribution and 0.999 is the confidence level. Finally, ρ_j , the asset correlation function, is given by¹:

$$\rho_j = 0.12 * \left(\frac{1 - e^{-50PD_j}}{1 - e^{-50}} \right) + 0.24 * \left(1 - \frac{1 - e^{-50PD_j}}{1 - e^{-50}} \right)$$

As shown by Gordy (2003), the total economic capital is simply obtained by adding the individual capital charges. Recently, Phytin (2004) and Cespedes et al. (2006) have provided approximate closed form formulae, and Tasche (2005) has provided an asymptotic analytic formula for the Unconditional Portfolio Loss density (and, for the Value at Risk quantiles) in a context of multiple systemic (static) factors driving a structural form Portfolio Credit Risk model. However, as pointed out in Section 2, we consider a reduced form model of credit risk which is non-linear in the Gaussian common shocks (due to equation 9). Consequently, we need to resort to stochastic simulation to produce density forecast for default rates and for the Portfolio Loss. Moreover, given the few common shocks underlying the systemic component of the reduced form Portfolio Credit Risk model, we argue that the one hundred thousand replications associated with the projection equation (8) cover an exhaustive number of scenarios. In other words, the computational feasibility of the stochastic simulation experiment is enhanced relative to studies based upon the indirect method of forecasting and the simulation of common observable factors through a VAR model (see Pesaran et al., 2006) or through a univariate AR(2) model (see Virolainen, 2004). In these studies the number of common shocks is equal to the number of endogenous variables times the forecast horizon. Furthermore, we argue that a DF modelling approach is more feasible than a VAR or than a state space modelling approach (see Koopman and Lucas, 2005) if we want to model the joint

¹ The asset correlation function we consider is the one corresponding to a corporate portfolio

interaction between macro time series and several industry sectors default rates at different forecast horizon and there is a short time series data span available for the various default rates.

5 Forecast evaluation

In this section we describe how to obtain and evaluate the forecasts for distressful scenarios. These are identified as the second largest sector specific default rate realisation in the forecast evaluation period (which is given by the last 20 sample observations). The probability forecasts for this event are produced as follows. First we compute the conditional projection associated with either equations (7) or (8) for 10000 scenarios. These projections are obtained by recursive estimation ending the first sample of observations in the second quarter of 2000 (and this will give the first prediction, one year ahead, for the second quarter of 2001). Then, we add one observation to the previous sample once we move ahead through the forecast evaluation period, producing projections accordingly. Specifically, for each observation in the forecast evaluation period, we produce 10000 forecast for one year ahead using either the indirect or the direct method as suggested by equations (7) and (8), respectively. Then, we count how many times the conditional projection is greater than the pre-specified threshold (e.g. the second largest sector specific default rate realisation in the forecast evaluation period). We label this number $proj_distress_j$ and we divide $proj_distress_j$ by 10000. This ratio gives the probability forecast of financial distress (relative to the forecast evaluation period examined, which ranges from the second quarter of 2001 to the first quarter of 2006). Using the aforementioned recursive method of estimation for the whole forecast evaluation period, we also compute probability forecasts using, first, the following naïve predictor for the probit transform of a sector specific default rate:

$$\hat{y}_{t+4}^i = \mu_t^i + \sigma_t^i \eta_{t+4}^i \quad (12)$$

where μ_t^i and σ_t^i are the sample mean and sample deviation of the proxy of default rates for sector i (conditional on the sample of observations ending at time t) and the η 's are Gaussian white noise random draws. Then, we compute the standard cumulative normal distribution $\Phi\left(\hat{y}_{t+4}^i\right)$ to obtain the conditional projection of the default rate level. We also consider the probability forecasts (conditional on the information set ending at time t) obtained from the following linear factor model:

$$\hat{y}_{t+4}^i = \beta_{0,t} + \beta_{1,t}gdp + \beta_{2,t}int_real + \sigma_{idios,t}\eta_{t+4} \quad (13)$$

where the β 's have been obtained using a sample of observations ending at time t and running an OLS regression of the probit transform of default rates for sector i on the GDP growth rate and on the one month real interest rate (using the ex post inflation rate). The simulation of the two observable common factors is carried by assuming, for each of them, a univariate AR(2) in line with Virolainen (2004), and with Credit Portfolio View (see Wilson, 1997), and by using the recursive substitution procedure characterising the indirect method of prediction. Finally, $\sigma_{idios,t}$ is the sample standard deviation of the residual from the above OLS regression and the η 's are Gaussian white noise random draws. Then, we compute the standard cumulative normal distribution $\Phi\left(\hat{y}_{t+4}^i\right)$ to obtain the conditional projection of the default rate level.

Finally, we use the following indicators of forecast accuracy:

$$QPS = \frac{1}{T} \sum_{t=1}^T 2(P_t - R_t)^2 \quad (14)$$

$$LPS = -\frac{1}{T} \sum_{t=1}^T [(1 - R_t) \ln(1 - P_t) + R_t \ln(P_t)] \quad (15)$$

where P_t and R_t are the probability forecast and the actual realisation of the variable one is interested in predicting. The QPS score ranges from 0 to 2, with 0 being perfect accuracy. The second one ranges from 0 to ∞ . LPS and QPS imply different loss functions with large mistakes more heavily penalized under LPS.

6. Empirical analysis

6.1 Data

We consider a corporate portfolio, and the obligors with marginal exposure have been grouped in homogenous clusters in terms of rating and economic sector.

The data span (quarterly frequency) under investigation starts from the first period data on default rates became available, that is, the first quarter of 1990, and it ends on the first quarter of 2006. In total, we have a dataset with 103 variables and these variables are, first, the 23 sector specific proxies of defaults rates, plus a proxy of the aggregate default rate for the Italian economy. The data

are published by the Bank of Italy, and they are computed as the ratio of the change (over a quarter) in the stock of non performing loans to the stock of performing loans existing at the beginning of the quarter. While our focus is on industry sector specific default rates, Marotta et al. (2005) use Italian proxies of default rates for three macro-regions: South, Centre and North of Italy, and these data are also disaggregated into default rates proxies corresponding to small, medium and large exposures. The other series included in the dataset are aggregate and disaggregate consumer and producer prices, aggregate and disaggregate data on gross domestic product and industrial production, data on sales and orders. Finally, we also include data on the term structure of interest rates. For a more detailed description of the data and their transformation, see the Appendix. Finally, each transformed series in the dataset has been standardised to have zero mean and unit variance, before applying principal component analysis.

6.2 Empirical Evidence: test for unit root on default rates and in-sample fit of DF model

The main focus of this paper is the empirical analysis of sector specific default rates proxies for the Italian economy. Therefore, it is important, first, to investigate the order of integration of this set of variables. We carry two type of unit root test. First, we use the univariate ADF test developed by Dickey and Fuller (1979) for the null of unit root for each of the sector specific default rates. The results from Table 1 suggest that default rates are stationary only after applying a first difference transformation. Then given the low power of the ADF unit root and, given the use, in this paper, of a Dynamic Factor model fitted to a large dataset for the purpose of forecasting and Portfolio Credit Risk modelling, we use the PANIC test recently developed by Bai and Ng (2004) which tests separately for the null of unit root in the factors driving the common component of the full dataset (which includes all the 103 constituents) and in the idiosyncratic component. We apply the PANIC test to the 103 variables dataset where all the series (except the default rates proxies, which are in levels) have been subject to standard transformation (see the appendix for more details regarding the transformation) for the purpose of factor analysis. The PANIC test results can be described as follows. First, from Table 2, according to MQ_c test statistics for the null of unit root (with only intercept) developed by Bai and Ng (2004), any factor model with the number of principal components varying from six to one (according to the sequential order testing suggested by the authors) is shown to be stationary, given that the null of unit root is always rejected (see the 1% critical values in the footnote of Table 2). Also, the χ^2 and the standardised Gaussian version of the pooled test on the idiosyncratic component (obtained by subtracting, from the actual time series, the common component, corresponding to the different number of principal components) show evidence of stationary idiosyncratic component for each variable in the dataset considered. To

summarise, contrary to the univariate ADF unit root tests, the PANIC procedure suggest that the level of the sector specific default rates proxies is stationary. Therefore, we include the level of default rates proxies in the dataset from which we extract the principal components to carry forecasting and Portfolio Credit Risk analysis.

As argued in Forni et al. (2005), a VAR(1) specification for the static factors provides a parsimonious characterisation of the rich dynamics in a large dataset. Given that, in this paper, the dimension q for the dynamic factor is fixed either to one or to two, and given the small time series dimension of the dataset considered (which implies that we need to cope with a lack of degrees of freedom when fitting a VAR(1) to the estimated principal components), we concentrate on different DF model specifications corresponding to four, five and six principal components, each with either one or two dynamic factors.

As for in sample forecasting performance, we focus on adjusted R^2 , obtained from OLS regression of each of the observables in the large dataset (including 103 variables) on the principal components. The mean values of the adjusted R^2 for the whole dataset corresponding to four, five and six principal components are 0.44, 0.48, 0.51, respectively. Furthermore, the mean values of the adjusted R^2 for the 24 default rates constituents of the whole dataset corresponding to four, five and six principal components are 0.38, 0.40, 0.42, respectively.

6.3 Empirical Evidence: forecast evaluation

An inspection of the average QPS and LPS scores in Tables 3-4 shows that the out of sample probability forecast performance of the indirect method is enhanced when we move from one dynamic factor (see from the eight column to the tenth column of Tables 3 and 4) to a two dynamic factors (see from the eleventh column to the thirteenth column of Tables 3 and 4) model specification. Specifically, the average QPS score for the dynamic forecasts through one dynamic factor varies between 0.409 and 0.433, whereas the average QPS score associated with the dynamic forecasts through two dynamic factors vary between 0.399 and 0.402. We also find that the direct method of forecasting through (static factors) outperforms the indirect method of prediction (through dynamic factors). Specifically, the QPS scores (averaged across the various sectors) associated with the direct method of forecasting through four, five and six principal components are 0.339, 0.358, 0.374, respectively. Similar findings are associated with the LPS scores (averaged across the various sectors). The direct method of forecasting through four, five and six principal components is the best performer, given mean values of the LPS varying between equal to 0.521, 0.537, 0.554, respectively. These values are lower than both the (average) LPS scores corresponding to the indirect method of prediction through one dynamic factor and four, five and

six principal components (the scores are 0.821, 0.759, 0.751, respectively), and the (average) LPS scores corresponding to the indirect method of prediction either through one dynamic factor (with values ranging between 0.638 and 0.697) or through two dynamic factors (with values ranging between 0.603 and 0.625).

Moreover, on average, the out of sample probability forecast performance of the Dynamic Factor model (either through the direct or through the indirect method of projection) is more accurate than the one associated with a naïve predictor which has an (average) QPS equal to 0.625 and an (average) LPS equal to 0.864. In terms of QPS scores, few are the industry sectors where the naïve predictor outperforms the principal component model (when using the indirect method of forecasting through the use of either one or two dynamic factors) and they are: Electric Materials, Int. Transport Services and Communication Services. In terms of LPS scores, the industry sectors where the naïve predictor outperforms the principal component model (when using the indirect method of forecasting through the use of either one or two dynamic factors) are: Chemicals, Electric Materials, Int. Transport Services. The direct and indirect method of forecasting through principal components also outperforms a Credit Portfolio View reduced form type of modelling approach (see also Virolainen, 2004) as described in equation (13), which exhibit average QPS and LPS scores equal to 0.489 and 0.694, respectively.

6.4 Portfolio Credit Risk estimation

We now use the whole information set (e.g. the whole sample period ending in the first quarter of 2006) to provide measures of one year ahead forecast uncertainty. Specifically, we are after measures of portfolio credit risk (via reduced form modelling) which can be obtained by analysing the unconditional portfolio loss density, and, in particular, by concentrating on few moments of this density function. Once the expected loss is obtained by computing the mean of the overall Portfolio Loss density, the difference between the 99.9% percentile (as suggested by Basel 2) and the expected loss, gives the unexpected loss (economic capital). If the forecast horizon is a year, then the unexpected loss predicts the minimum loss (above the expected one) that can occur with 0.1% probability. Finally, if such an extreme event occurs, it is useful to compute the expected shortfall, given by the mean of the Portfolio Loss density, beyond the 99.9% percentile. This measure gives the loss that is likely to occur in presence of extreme event with 0.1% probability to occur. Assuming a constant recovery rate, the expected portfolio loss depends only on the unconditional PD's (and on the different exposures) and not on the factor model specification. Therefore, the simulation experiment, through equation (9), allows to keep the simulated portfolio expected loss invariant across the different model specification and its value is equal to 0.304%, which can be

obtained by computing the average of the exposures weighted by their corresponding unconditional PD's.

Our primary focus is to assess whether, for a given degree of heterogeneity in the exposures and in the unconditional probability of defaults, there is any benefit in terms of credit risk diversification (relative to the Gordy (2003) analytic formula for the unexpected loss) occurs once we consider different multifactor model for the purpose of Portfolio Credit Risk analysis. Therefore, we now turn our focus on the interpretation of the empirical results in Table 5, 6 and 7 which provide the outcome of reduced form Portfolio Credit Risk modelling. The Basel II measure of the unexpected loss, obtained from the analytic solution (for a structural form Portfolio Credit Risk model) provided by Gordy (2003) is equal to 4.70% of total exposure. This value, by inspecting Tables 5 and 6, is bigger than the one corresponding to the different predictions (either through the direct or through the indirect method of forecasting) associated with various multifactor versions of the DF model and obtained through the stochastic simulation experiment described in section 4. We can interpret these findings in line with Servigny and Renault (2002) which show that the implied pair wise asset value correlation from default correlation (which in our study is based upon an h step ahead projection) are low. We expect these values to be lower than the asset value correlation (which averages 20%) underlying the Basel 2 analytic formula for the economic capital. The findings in Tables 6 and 7 suggest that the number of factors underlying default correlation play an important role (especially when we use the indirect method of forecasting)². More specifically, by introducing dynamics and multiple factors we allow for a considerable degree of heterogeneity in the factor loadings, which tend to decrease Portfolio Credit Risk. On the other hand, dynamics and multiple factors have an effect in the opposite direction, given that they introduce a degree of innovation uncertainty varying across different forecast horizon. The innovation uncertainty associated with the indirect method of forecasting is due to a covariance matrix (for the forecast errors) which is a linear combination of four quadratic forms (see equation 7), that is $y_{t+4|t,U}^i = C^{i*} [\Gamma^4 \Gamma^4 ' + \Gamma^3 RR' \Gamma^3 ' + \Gamma^2 RR' \Gamma^2 ' + \Gamma RR' \Gamma ' + RR'] C^{i*} ' ,$ where C^{i*} is a matrix whose coefficients are given by un-standardised factor loadings. The innovation uncertainty associated with the direct method of forecasting is due to only one quadratic form (see equation 8), $A_4^{i*} A_4^{i*} ' ,$ where A^i are the un-standardised factor loadings, which depend upon the chosen forecast horizon.

² We also argue that we cannot explain our findings in line with the studies of Phytkin (2004) and of Cespedes et al. (2006), e.g. by taking into account the existence of less than perfectly correlated multiple common factors. The main reason is that our is a reduced form model of Portfolio Credit Risk, whereas the one developed by Phytkin (2004) and Cespedes et al. (2006) are structural form models. Furthermore, the aforementioned studies are “static”, given that there is no dynamics in the factors underlying of the unobservable firm asset value.

In this study, the differences between the Dynamic Factor model and the Basel 2 analytic formula lie on factor loadings heterogeneity and on innovation uncertainty. The degree of factor loadings heterogeneity associated with the Dynamic Factor model (and, we argue, the heterogeneity in the loadings underlying the implied asset value correlation) more than offset the corresponding degree of innovation uncertainty. This offsetting mechanism dominates the degree of heterogeneity on factor loadings coefficients underlying the Basel 2 analytic formula.

Given the aforementioned implications that direct and indirect method of prediction have on the covariance matrix of the forecast errors, we find that the degree of innovation uncertainty and, consequently, the value of the unexpected loss, associated with the indirect method of forecasting (especially when focussing on two dynamic factors, see Table 7) is higher than the one corresponding to direct method. This effect also contributes to a (left) skewed portfolio loss density, hence to an higher unexpected loss and expected shortfall. In particular, values of the unexpected loss associated to the direct method direct method of prediction are between 0.478 and 0.494, whereas values of the unexpected loss derived from the indirect method are, on average, equal to 1.511%. Also, when comparing Table 6 with Table 7, we find that, for a given number of principal components (proxies of the static factors), an increase in the number of dynamic factors, implies a decrease in the degree of dynamic heterogeneity (given that the number of lags of the dynamic factors drops). Specifically, the unexpected loss derived from shocks to a single dynamic factor varies between 0.400% and 1.206%, whereas the unexpected loss derived from shocks to two dynamic factors varies between 1.406% and 3.456%. A similar pattern can be observed for the expected shortfall.

7 Conclusions

This paper employs a Dynamic Factor model, DF, along the lines of Stock and Watson (2002), to study Italian industry sector specific default rates proxies. Given the short time series data span of default rates (e.g. 65 quarterly observations, available since 1990), default correlation and portfolio loss density modelling is obtained through the estimation and the simulation of an handful of principal components underlying the dynamics of a large dataset of 103 constituents including both default data and macroeconomic variables. Preliminary analysis shows that, according to the PANIC test developed by Bai and Ng (2004), the default rates proxies are stationary in levels. The modelling approach we use is of a reduced form type and the simulation of the DF model allows to obtain the density forecast of defaults by employing both a direct and an indirect method of

prediction. While the former method generates density predictions using shocks to principal components (proxy of the static factors), the latter generates density predictions using shocks to the dynamic factors. In a first stage of the analysis, the direct method is shown to be the best performer in terms of the out of sample probability forecast performance (regarding financial distressful events). In a second stage of the analysis, we implement stochastic simulation, using as inputs the Dynamic Factor model parameter estimates and a specific portfolio loan exposure dataset, and the sample mean value of each industry sector default rate proxy as the unconditional probability of default (sector specific). The simulation of the unconditional loan portfolio loss density through principal components, suggests a value of the minimum capital requirements (through the cycle) lower than the one obtained by the analytic formula recommended by Basel 2. We also find that the degree of (innovation) uncertainty and, consequently, the value of the unexpected loss and the expected shortfall associated with the indirect method of forecasting (especially when focussing on two dynamic factor) is higher than the one corresponding to the direct method. Finally, when using the indirect method of forecasting we obtain that an increase in the number of dynamic factors (for a given number of principal components) increases Portfolio Credit Risk.

References

- Alves, I. (2004) "Sectoral fragility: factors and dynamics", *BIS Papers* no. 22.
- Bai, J. and Ng, S. (2004) "A PANIC Attack on Unit Roots and Cointegration". *Econometrica*, 72 (4), 1127-1177.
- Caling, K., Jacobson T., Lind, J. and K. Roszbach (2006): "Corporate Credit Risk Modeling and the Macroeconomy". *Journal of Banking and Finance*, forthcoming.
- Céspedes, J.C.G, Herrero, J., Kreinin, A. and D. Rosen (2006) "A Simple Multi-Factor "Factor Adjustment" for the Treatment of Credit Capital Diversification", *Journal of Credit Risk*, forthcoming
- Dickey, D. A. and Fuller, W. A. (1979), "Distribution of the Estimators for Autoregressive Time Series with a Unit Root", *Journal of the American Statistical Association* 74, 427–431.
- Elsinger, Helmut, Alfred Lehar, and Martin Summer, 2002, "Risk Assessment for Banking Systems," *Österreichische Nationalbank Working Paper* No. 79.
- Finger, C. (1999) "Conditional approaches for CreditMetrics portfolio distributions". *CreditMetrics Monitor* 1, 14–33.
- Forni, M., Giannone D., Lippi, M., Reichlin L. (2005): "Opening the Black Box: structural factor model versus structural VAR models", *Universite Libre de Bruxelles*, mimeo

Gordy, M. (2003): “A Risk-Factor Model Foundation for Ratings-Based Bank Capital Rules”, *Journal of Financial Intermediation*, vol. 12 (July 2003), pp. 199-232.

Gupton, G., Finger C., and M. Bhatia. (1997). CreditMetrics™ — Technical Document. J.P. Morgan, New York.

Hamerle, A., Liebig T., and D. Rosch (2003): “Credit Risk Factor Modeling and the Basel II IRB Approach”, *Deutsche Bundesbank working paper*, no 02/2003.

Hamerle, A. Liebig, T. and Scheule, H. (2004): “Forecasting Credit Portfolio Risk” *Deutsche Bundesbank working paper*, no 02/2003.

Hanson, S.G., Pesaran H., and Schuermann T. (2005): “Firm heterogeneity and credit risk diversification”, CESifo working paper series no. 1531

Hoggarth, G., Sorensen, S. and L. Zicchino (2005), “Stress Tests of UK Banks Using a VAR Approach,” *Bank of England Working Paper* No. 282.

Koopman, S.J., Lucas, A. and P. Klaassen (2005): “Empirical Credit Cycles and Capital Buffer Formation”, *Journal of Banking and Finance*, 29 (12), 3159-3179.

Koopman, S.J., and Lucas, A. (2005): “Business and default cycles for credit risk”, *Journal of Applied Econometrics*, 20(2), 311-323.

Lucas, A., P. Klaassen, P. Spreij, and S. Straetmans (2001). “An analytic approach to credit risk of large corporate bond and loan portfolios”. *Journal of Banking and Finance* 25, 1635–1664.

Marcellino, M., Stock, J. H. & Watson, M. W. (2005). A comparison of direct and iterated multistep ar methods for forecasting macroeconomic time series, *Journal of Econometrics*, forthcoming.

Marotta, G., Pederzoli, C., and Torricelli, C.(2005): “Forward looking estimation of default probabilities with Italian data”, *Universita’ di Modena e Reggio Emilia, Dipartimento di Economia Politica, working paper* no 0504..

Merton, R. (1974). “On the pricing of corporate debt: the risk structure of interest rates”. *Journal of Finance* 29, 449–470.

Pain, D. (2003) “The Provisioning Experience of the Major UK Banks: A Small Panel investigation.” *Bank of England Working Paper* No. 177.

Pesaran, H., Schuermann, T., Treutler, B.J. and Weiner, S.W. (2006): “Macroeconomics Dynamics and Credit risk: a global perspective”, *Journal of Money, Credit and Banking*, 38(5), 1211-1262

Pykhtin, M. (2004) “Multi-factor adjustment”. *Risk*, 17, 85–90.

Schonbucher, P. (2000): “Factor models for portfolio credit risk” Bonn University working paper

Servigny, A. and Renault, O. (2002): “Default correlation: empirical evidence”, mimeo

Stock and Watson: “Macroeconomic Forecasting using diffusion indices”, *Journal of Business and Economic Statistics*, 20(2), 147-162

Tasche D. (2005): “ *Measuring Diversification in an Asymptotic Multi-Factor Framework*”, Deutsche Bundesbank working paper.

Vasicek O., (2002), “*Loan Portfolio Value*”, *Risk*, December, 160-162.

Violainen, K. (2004): “Macro stress testing with a macroeconomic credit risk model for Finland”, *Bank of Finland working paper*, 18-2004.

Wilson, T.C. (1997a): “Portfolio Credit Risk (I)”, *Risk*, September. (Reprinted in *Credit Risk Models and Management*. 2004, 2nd edition, edited by David Shimko, Risk Books).

Wilson, T.C. (1997b) “Portfolio Credit Risk (I)”, *Risk*, October. (Reprinted in *Credit Risk Models and Management*. 2004, 2nd edition, edited by David Shimko, Risk Books).

Table 1: ADF unit root test on default rates

Sector	ADF t –statistic on levels	ADF t –statistic on first diff
Default rate: Agriculture and fishing	-1.14	-3.49
Default rate: Energy	-1.06	-5.36
Default rate : Minerals and e iron and non iron metals	-2.12	-3.92
Default rate: Default rate: Minerals and non metals based materials	-0.92	-6.22
Default rate: Chemicals	-1.55	-3.82
Default rate : Metals	-2.31	-3.08
Default rate : Agriculture and Industry Machines	-1.84	-3.82
Default rate: Office Machines	-1.91	-5.89
Default rate: Electric Materials	-1.37	-4.06
Default rate: Transport Materials	-1.43	-4.98
Default rate: Food	-1.83	-3.65
Default rate: Textiles	-2.90	-3.80
Default rate: Paper	-1.77	-3.80
Default rate: Rubber and Plastic Goods	-2.11	-4.00
Default rate: Other industrials good	-1.28	-3.63
Default rate: Construction	-0.90	-4.25
Default rate: Commerce and refurbishing services	-0.89	-3.62
Default rate: Hotel and restaurants	-0.99	-3.00
Default rate: Internal Transport Services	-2.20	-5.44
Default rate: Naval and airplane transport services	-1.64	-3.83
Default rate: Services connected to Transports	-1.64	-3.83
Default rate: Communication services	-3.18	-4.97
Default rate: Other services for sales	-0.86	-3.96
Default rate: Aggregate	-1.24	-3.64

Note: The lag order for the ADF regression is equal to $4*(T/100)^{1/4}$. The 5% and 10% critical values for ADF test are -2.82, and -2.52, respectively.

Table 2: PANIC test on the 103 variables dataset with default rates in levels

	MQ_c	
Model with 6 Factors	-87.63	
Model with 5 Factors	-88.77	
Model with 4 Factors	-81.46	
Model with 3 Factors	-76.90	
Model with 2 Factors	-66.11	
Model with 1 Factor	-68.93	
	χ^2	$N(0,1)$
Pooled ADF test (with no const) on ξ ; Model with 6 Factors	678.84	23.29
Pooled ADF test (with no const) on ξ ; Model with 5 Factors	694.73	24.07
Pooled ADF test (with no const) on ξ ; Model with 4 Factors	726.20	25.62
Pooled ADF test (with no const) on ξ ; Model with 3 Factors	718.60	25.25
Pooled ADF test (with no const) on ξ ; Model with 2 Factors	725.53	25.59
Pooled ADF test (with no const) on ξ ; Model with 1 Factor	869.79	32.70

Note: From Table I in Bai and Ng (2004), the 1% critical values for the MQ_c test for the null of unit root (with only intercept) in the common component ranging from one to six factors are: -20.15,-31.61,-41.06,-48.5,-58.38, -66.97, respectively. In the columns labelled χ^2 and $N(0,1)$, we report the the chi-square (with two degrees of freedom) and the standardised Gaussian statistics for the Pooled ADF test the idiosyncratic component for each of the observables

Table 3: QPS scores

Sector	Naive	CPW	4pc; direct	5pc; direct	6pc; direct	4pc; 1df	5pc; 1df	6pc; 1df	4pc; 2df	5pc; 2df	6pc; 2df
Default rate: Agriculture and fishing	0.935	0.669	0.417	0.420	0.437	0.467	0.504	0.534	0.474	0.504	0.522
Default rate: Energy	0.601	0.435	0.305	0.373	0.393	0.305	0.293	0.295	0.339	0.342	0.346
Default rate : Min. and iron and non iron metals	0.528	0.288	0.213	0.328	0.352	0.179	0.174	0.183	0.198	0.206	0.205
Default rate: Min. and non metals based materials	0.887	0.626	0.512	0.517	0.535	0.497	0.519	0.529	0.495	0.514	0.523
Default rate: Chemicals	0.258	0.318	0.196	0.184	0.182	0.199	0.191	0.202	0.199	0.186	0.186
Default rate : Metals	0.662	0.501	0.329	0.362	0.407	0.321	0.360	0.380	0.358	0.390	0.397
Default rate : Agr. and Ind. Machines	0.319	0.370	0.222	0.272	0.314	0.188	0.189	0.215	0.206	0.215	0.234
Default rate: Off. Machines	0.262	0.396	0.186	0.184	0.193	0.195	0.196	0.220	0.255	0.261	0.254
Default rate: Elec. Mat.	0.194	0.208	0.187	0.185	0.182	0.199	0.200	0.200	0.199	0.207	0.208
Default rate: Transp. Mat.	0.196	0.238	0.181	0.192	0.212	0.182	0.173	0.148	0.191	0.187	0.179
Default rate: Food	0.558	0.479	0.322	0.316	0.324	0.229	0.276	0.286	0.281	0.330	0.340
Default rate: Textiles	0.508	0.485	0.303	0.373	0.429	0.290	0.277	0.308	0.302	0.314	0.324
Default rate: Paper	0.656	0.498	0.509	0.526	0.540	0.322	0.368	0.409	0.359	0.396	0.413
Default rate: Rubber and Plastic Goods	0.633	0.490	0.299	0.355	0.373	0.231	0.213	0.232	0.349	0.350	0.352
Default rate: Oth. Ind. good	0.586	0.492	0.329	0.358	0.370	0.251	0.265	0.263	0.303	0.3261	0.312
Default rate: Construction	1.288	0.571	0.692	0.664	0.631	1.170	1.134	1.225	0.967	0.863	0.832
Default rate: Comm. and ref. services	0.924	0.686	0.415	0.427	0.435	0.477	0.499	0.517	0.485	0.492	0.500
Default rate: Hotel and restaurants	1.1760	0.963	0.544	0.551	0.563	1.121	1.002	1.114	0.873	0.818	0.841
Default rate: Int. Transp Services	0.189	0.381	0.213	0.236	0.242	0.185	0.198	0.194	0.251	0.250	0.235
Default rate: Naval and airplane transp. Services	0.186	0.166	0.165	0.171	0.167	0.185	0.183	0.200	0.163	0.180	0.180
Default rate: Services connected to Transports	0.566	0.448	0.228	0.257	0.338	0.202	0.204	0.233	0.307	0.308	0.305
Default rate: Communication services	0.217	0.264	0.188	0.164	0.169	0.201	0.203	0.236	0.235	0.229	0.252
Default rate: Other services for sales	1.332	0.767	0.569	0.561	0.565	1.240	1.178	1.165	0.922	0.889	0.868
Default rate: Aggregate	1.341	1.005	0.603	0.607	0.621	1.050	1.021	1.117	0.862	0.837	0.846
Arithmetic Average	0.625	0.489	0.339	0.358	0.374	0.412	0.409	0.433	0.399	0.400	0.402

Note: In the second and third column we report the QPS scores associated with a naive predictor, as pointed in equation (12) and associated with a Credit Portfolio View approach, as pointed in equation (13). From the fifth to the seventh column, we report the QPS scores associated with direct method of forecasting through four, five and six principal components, respectively. The remaining columns report the QPS scores associated with the indirect method, using one dynamic or two dynamic factors, and four, five, six principal components, respectively.

Table 4: LPS scores

Sector	Naive	CPW	4pc; direct	5pc; direct	6pc; direct	4pc; 1df	5pc; 1df	6pc; 1df	4pc; 2df	5pc; 2df	6pc; 2df
Default rate: Agriculture and fishing	1.169	0.873	0.611	0.614	0.632	0.659	0.697	0.728	0.667	0.697	0.716
Default rate: Energy	0.794	0.628	0.494	0.562	0.585	0.495	0.482	0.484	0.530	0.532	0.536
Default rate : Min. and iron and non iron metals	0.721	0.473	0.379	0.513	0.539	0.313	0.311	0.319	0.362	0.370	0.362
Default rate: Min. and non metals based materials	1.110	0.821	0.706	0.711	0.731	0.690	0.712	0.722	0.688	0.708	0.716
Default rate: Chemicals	0.440	0.507	0.454	0.379	0.353	0.743	0.618	0.804	0.699	0.477	0.628
Default rate : Metals	0.858	0.694	0.517	0.551	0.597	0.510	0.551	0.571	0.549	0.582	0.589
Default rate : Agr. and Ind. Machines	0.508	0.560	0.389	0.453	0.499	0.349	0.336	0.369	0.374	0.378	0.397
Default rate: Off. Machines	0.443	0.588	0.338	0.331	0.348	0.355	0.353	0.385	0.435	0.442	0.434
Default rate: Elec. Mat.	0.434	0.372	0.348	0.336	0.329	0.921	0.898	0.927	0.700	0.660	0.792
Default rate: Transp. Mat.	0.355	0.415	0.328	0.341	0.378	0.328	0.290	0.244	0.342	0.341	0.326
Default rate: Food	0.751	0.672	0.504	0.496	0.507	0.391	0.456	0.468	0.462	0.519	0.528
Default rate: Textiles	0.701	0.678	0.487	0.561	0.620	0.475	0.457	0.494	0.489	0.502	0.512
Default rate: Paper	0.851	0.691	0.706	0.724	0.736	0.510	0.558	0.601	0.550	0.588	0.605
Default rate: Rubber and Plastic Goods	0.827	0.683	0.482	0.542	0.562	0.399	0.363	0.393	0.539	0.541	0.542
Default rate: Oth. Ind. good	0.780	0.685	0.518	0.546	0.559	0.425	0.443	0.440	0.488	0.515	0.496
Default rate: Construction	1.723	0.765	0.902	0.872	0.830	2.123	1.512	1.902	1.479	1.089	1.054
Default rate: Comm. and ref. services	1.155	0.883	0.606	0.619	0.627	0.670	0.692	0.710	0.678	0.685	0.694
Default rate: Hotel and restaurants	1.508	1.269	0.739	0.746	0.759	1.476	1.284	1.488	1.102	1.031	1.065
Default rate: Int. Transp Services	0.377	0.573	0.379	0.412	0.415	0.336	0.358	0.350	0.430	0.429	0.409
Default rate: Naval and airplane transp. Services	0.345	0.298	0.293	0.308	0.303	0.346	0.331	0.514	0.282	0.324	0.320
Default rate: Services connected to Transports	0.759	0.641	0.402	0.436	0.521	0.368	0.364	0.405	0.494	0.495	0.491
Default rate: Communication services	0.454	0.472	0.349	0.276	0.291	0.364	0.367	0.413	0.411	0.403	0.431
Default rate: Other services for sales	1.828	0.996	0.763	0.755	0.759	1.694	1.570	1.550	0.922	1.115	1.097
Default rate: Aggregate	1.851	1.420	0.800	0.804	0.818	1.344	1.296	1.453	1.088	1.053	1.066
Arithmetic Average	0.864	0.694	0.521	0.537	0.554	0.679	0.638	0.697	0.625	0.603	0.617

Note: In the second and third column we report the LPS scores associated with a naive predictor, as pointed in equation (12) and associated with a Credit Portfolio View approach, as pointed in equation (13). From the fifth to the seventh column, we report the LPS scores associated with direct method of forecasting through four, five and six principal components, respectively. The remaining columns report the LPS scores associated with the indirect method, using one dynamic or two dynamic factors, and four, five, six principal components, respectively.

Table 5: Credit Portfolio Risk corresponding to direct forecasts through DF model

	4 static factors	5 static factors	6 static factors
Expected Loss	0.304	0.304	0.304
99.9% VaR	0.796	0.782	0.799
Unexpected Loss	0.491	0.478	0.494
Expected Shortfall	0.874	0.855	0.873

Note: numbers are in percentages of total exposure

Table 6: Credit Portfolio Risk corresponding to indirect forecasts through DF model: the case of one dynamic factor

	4 static factors	5 static factors	6 static factors
Expected Loss	0.304	0.304	0.304
99.9% VaR	0.705	1.510	1.489
Unexpected Loss	0.400	1.206	1.184
Expected Shortfall	0.764	1.755	1.182

Note: numbers are in percentages of total exposure

Table 7: Credit Portfolio Risk corresponding to indirect forecasts through DF model: the case of two dynamic factors

	4 static factors	5 static factors	6 static factors
Expected Loss	0.304	0.304	0.304
99.9% VaR	1.711	3.760	1.723
Unexpected Loss	1.406	3.456	1.419
Expected Shortfall	1.960	4.562	1.999

Note: numbers are in percentages of total exposure

DATA

Code	Data description	Transformation
EUR001M	Euribor 1 mesi	3
EUR003M	Euribor 3 mesi	3
EUR006M	Euribor 6 mesi	3
ILRSGVTG	Italy rendistato govt bond	3
ITISCOKE	COKE SA SALES	3
ITISELEC	ELECTRICS SA SALES	3
ITISFOOD	FOOD SALES	3
ITISFSAT	FOREIGN SALES SA	3
ITISLEAT	LEATHER SA SALES	3
ITISMACH	MACHINERY SA SALES	3
ITISMANF	MANUFACTURING SA SALES	3
ITISMETL	METALS SA SALES	3
ITISMINE	MINERALS SA SALES	3
ITISNMET	NON METALS SA SALES	3
ITISNSAT	DOMESTIC SALES SA	3
ITISOTHR	OTHERS SA SALES	3
ITISPAPR	PAPER SA SALES	3
ITISRUBB	RUBBER SA SALES	3
ITISSCO	CONSUPTION GOODS SA SALES	3
ITISSEN	ENERGY SA SALES	3
ITISSIN	INVESTMENT GOODS SA SALES	3
ITISSINT	INTERM GOODS SA SALES	3
ITISTEXT	TEXTILES SA SALES	3
ITISTRAN	TRANSPORT SA SALES	3
ITISTSAT	TOTAL SALES SA	3
ITISWOOD	WOOD SA SALES	3
ITORFSAL	ITALY FOREIGN INDUSTRIAL ORDER SA	3
ITORNSAL	ITALY NATIONAL INDUSTRIAL ORDER SA	3
ITORTSAL	ITALY INDUSTRIAL ORDER SA	3
ITPIRES	ITALY REAL GDP EXPORTS SA WDA	3
ITPIRIS	ITALY REAL GDP IMPORTS SA WDA	3
ITPIRLS	ITALY REAL GDP SA WDA	3
ITPIRMS	ITALY REAL GDP MACHINERY SA WDA	3
ITPIRNS	ITALY REAL GDP INVESTMENTS SA WDA	3
ITPIROS	ITALY REAL GDP CONSTRUCTION SA WDA	3
ITPIRPCS	ITALY REAL GDP PRIVATE CONSUMPTION SA WDA	3
ITPIRSS	ITALY REAL GDP CONSTANT PRICE CHANGE IN STOCKS SA WDA	3
ITPIRTC	ITALY REAL GDP CONSUMPTION SA WDA	3
ITPIRTCW	ITALY REAL GDP TRANSPORTS SA WDA	3
ITPIRUCS	ITALY REAL GDP PUBLIC CONSUMPTION SA WDA	3
ITPRENS	ITALY INDUSTRIAL PRODUCTION ENERGY SA	3
ITPRINS	ITALY INDUSTRIAL PRODUCTION INVESTMENT GOODS SA	3
ITPRITS	ITALY INDUSTRIAL PRODUCTION INTERMED GOODS SA	3
ITPRSAN	ITALY INDUSTRIAL PRODUCTION SA	3
ITPRSCI	ITALY INDUSTRIAL PRODUCTION CHEMICALS SA	3
ITPRSDI	ITALY INDUSTRIAL PRODUCTION FOOD SA	3
ITPRSEI	ITALY INDUSTRIAL PRODUCTION ELECTRICS SA	3
ITPRSFI	ITALY INDUSTRIAL PRODUCTION MANUFACTURING SA	3
ITPRSGI	ITALY INDUSTRIAL PRODUCTION ENERGY SA	3
ITPRSHI	ITALY INDUSTRIAL PRODUCTION MACHINERY SA	3
ITPRSKI	ITALY INDUSTRIAL PRODUCTION COKE SA	3

ITPRSLI	ITALY INDUSTRIAL PRODUCTION LEATHER SA	3
ITPRSNL	ITALY INDUSTRIAL PRODUCTION NON METALS SA	3
ITPRSOI	ITALY INDUSTRIAL PRODUCTION OTHER SA	3
ITPRSPI	ITALY INDUSTRIAL PRODUCTION PAPER SA	3
ITPRSRI	ITALY INDUSTRIAL PRODUCTION RUBBER SA	3
ITPRSSI	ITALY INDUSTRIAL PRODUCTION METALS SA	3
ITPRSTI	ITALY INDUSTRIAL PRODUCTION TEXTILES SA	3
ITPRSWI	ITALY INDUSTRIAL PRODUCTION WOOD SA	3
ITPRSXI	ITALY INDUSTRIAL PRODUCTION FURNITURE SA	3
CPALIT	ALL ITEM CPI ITALIA	4
CPCLITI	CLOTHING AND FOOTWEAR CPI ITALIA	4
CPCMITI	COMMUNICATIONS CPI ITALIA	4
CPEDITI	EDUCATION CPI ITALIA	4
CPENITI	ENERGY CPI ITALIA	4
CPEXITI	CORE CPI ITALIA	4
CPFDITI	FOOD CPI ITALIA	4
CPFNITI	FURNISHING CPI ITALIA	4
CPGGITI	GOODS CPI ITALIA	4
CPHLITI	HEALTH CPI ITALIA	4
CPHRITI	RESTURANT AND HOTELS CPI ITALIA	4
CPMSITI	MISCELLANEOUS CPI ITALIA	4
CPRNITI	RECREATION CPI ITALIA	4
CPTRITI	TRANSPORT CPI ITALIA	4
CPXNITI	EXCLUDING ENERGY CPI ITALIA	4
PPENIT	PPI ENERGY	4
PPMNIT	PPI MANUFACTURING ITALIA	4
PPNGIT	PPI NON DOURABLE GOODS ITALIA	4
051	Default rate: Agriculture and fishing	2
052	Default rate: Energy	2
053	Default rate : Minerals and e iron and non iron metals	2
054	Default rate: Minerals and non metals based materials	2
055	Default rate: Chemicals	2
056	Default rate : Metals	2
057	Default rate : Agriculture and Industry Machines	2
058	Default rate: Office Machines	2
059	Default rate: Electric Materials	2
060	Default rate: Transport Materials	2
061	Default rate: Food	2
062	Default rate: Textiles	2
063	Default rate: Paper	2
064	Default rate: Rubber and Plastic Goods	2
065	Default rate: Other industrials good	2
066	Default rate: Construction	2
067	Default rate: Commerce and refurbishing services	2
068	Default rate: Hotel and restaurants	2
069	Default rate: Internal Transport Services	2
070	Default rate: Naval and airplane transport services	2
071	Default rate: Services connected to Transports	2
072	Default rate: Communication services	2
073	Default rate: Other services for sales	2
000	Default rate: Aggregate	2

Note: In the third column, the number are associated to a specific transformation of each raw series. Specifically, the transformations are as follows: 2 = probit transform; 3 = first difference of the log level; 4 = first difference of the annualised growth rate ($(y_t - y_{t-4})/y_{t-4}$), where y is the log level of the time series. As for the interest rates (the first four series) variables in the second column, these are the transformed annualised rates, r , into quarterly gross rates, using $\frac{1}{4}[\log(1+r/100)]$. We then apply the first order difference transformation. Furthermore the raw data on the interest rates with one, three

and six months maturity are the RIBOR rates and the EURIBOR rates, from 1999 onwards. Italy rendista govt bond is the interest rate on government bonds with maturity over one year. Transformation 4 is for the prices series whose raw observations are not seasonally adjusted. Finally data for industrial production, GDP, sales and orders are in real values.

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